# MANONMANIAM SUNDARANAR UNIVERSITY TIRUNELVELI

# PG - COURSES - AFFILIATED COLLEGES

Course Structure for M.Sc Mathematics (Choice Based Credit System)

( with effect from the academic year 2017- 2018 onwards)

Sem .	Sub. No.	Subject Status	Subject Title	Contact Hrs./	Credit
(1)	(2)	(3)	(4)	Week (5)	S
		(3)			(6)
	12	Core - 11	Measure and Integration	6	4
	13	Core - 12	Topology – I	6	4
III	14	Core - 13	Advanced Algebra - I	5	4
111	15	Core - 14	Operations Research	5	4
	16	Core - 15	Research Methodology	4	4
		Elective – 2 (Any one)	<ol> <li>Algebraic Number Theory</li> <li>Calculus of Variation and Integral Equations</li> <li>Formal Languages and Automata Theory</li> </ol>	4	3
			Subtotal	30	23
	18	Core - 16	Functional Analysis	6	4
	19	Core - 17	Complex Analysis	6	4
IV	20	Core - 18	Advanced Algebra – II	5	4
1 4	21	Core - 19	Topology - II	5	4
	22	Core - 20	Project	8	8
			Subtotal	30	24
			Total	120	90

**Measure and Integration** (90 Hours)

L	T	P	С
2	4	0	4

### **Objective:**

- Gain the knowledge of measure spaces and measure interruption
- Understanding the concept of lesbeague measure, lesbeague integration and signed measure
- To provide the understanding of general measure spaces

### **Prerequisite:**

• Basic knowledge of differentiation, integration and continuity of real functions

### **Outcome:**

Knowledge gained about lesbeague theory and general measure spaces and their properties and construction.

**Unit I: LebesgueMeasure:**Lebesgue Measure – Lebesgue Outer Measure – The σ - Algebra of Lebesgue Measurable sets – Outer and Inner Approximation of Lebesgue Measurable sets – Countable Additivity, Continuity and the Borel – Cantelli Lemma.

**Chapter 2 :** Sec 2.1 - 2.5

**Problems : Chapter 2**: 1 - 12 and 17

L 16

Unit II: Lebesgue Measurable functions&Sequential pointwise Limits and related

**Theorems**: Lebesgue Measurable functions – Sums, Products and Compositions. Sequential pointwise Limits and Simple Approximation – Littlewood's Three Principles, Egoroff's Theorem and Lusin's Theorem

**Chapter 3 :** Sec 3.1 - 3.3 and

**Problems : Chapter 3**: 1-3

L 19

**Unit III:** Lebesgue Integration : Lebesgue Integration — The Riemann Integral — The Lebesgue Integral of a bounded Measurable function over a set of finite Measure — The Lebesgue Integral of a Measurable non — negative function.

**Chapter 4 :** Sec 4.1 - 4.3

### MSU / 2017-18 / PG -Colleges / M.Sc.(Mathematics ) / Semester -III / Ppr.no.12 / Core-11

Unit IV: Lebesgue Integral & Differentiablility: The general Lebesgue Integral – Countable Additivity and Continuity of Integration. Differentiation and Integration – Continuity of monotone functions – Differentiability of monotone function: Lebesgue's theorem – Functions of bounded variations: Jordan's theorem.

**Chapter 4 :**Sec 4.4 & 4.5 **Chapter 6 :** Sec 6.1 - 6.3

L 19

Unit V: Absolutely continuous functions &Signed Measures: Absolutely continuous functions – Integrating Derivatives: Differentiating Indefinite Integrals. Measure and Integration – Measures and Measurable sets – Signed Measures: The Hahn and Jordan Decompositions – The Caratheodory measure induced by an outer measure – The construction of outer measure

**Chapter 6 :** Sec 6.4 & 6.5 **Chapter 17 :** Sec : 17.1 - 17.4

L 20

**Text Book:** Real Analysis, Fourth Edition, H.L.Royden, P.M.Fitzpatrick, PHI Learning Private Ltd.

### **Book for Reference:**

Real Analysis Third Edition (PHI)-H.L.Royden Prentice hall of ofindia private limited –New Delhi (2006).

# MSU / 2017-18 / PG -Colleges / M.Sc.(Mathematics ) / Semester -III / Ppr.no.13 / Core-12

Topology I (90 Hours)

L	T	P	C
2	4	0	4

# **Objectives:**

- To distinguish space by means of Simple Topological invariants
- Gain the knowledge of constructing spaces by giving and to prove that in certain case, that the result is homeomorphic to standard spaces.

### **Prerequisite:**

• Basic knowledge in Set Theory and Analysis at Undergraduate level.

### **Outcome:**

Knowledge gained about Topological Spaces and the theories based on these spaces.

**Unit I:** Topological spaces : Topological spaces – Basis for a topology – The order

topology – The subspace topology- Closed sets and limit points.

**Chapter 2:** Sections: 12-14 and 16,17.

**Problems:** Section 13: 1, 4 and Section 16: 4, 6. Section 17: 1,11-13

L 16

**Unit II:** Product topology: The product topology on  $X \times Y$  – Continuous functions –

Product topology

**Chapter 2:** Section 15, 18,19.

**Problems:** Section 18: 2,3 and Section 19: 1-3.

L 18

**Unit III:** Metric Topology :Metric Topology

Chapter 2: Section 20, 21

**Problems:** Section 20:1-3 and section 21:1, 2.

L 19

**Unit IV: Some spaces in topological spaces:** Connected spaces – Compact spaces.

Chapter 3: Sections: 23,26

**Problems:** Section 23: 2-4 and Section 26: 3, 6.

L 20

**Unit V:** Compactness: Limit point compactness – Local compactness.

Chapter 3: Section 28, 29.

**Problems:** Section 29: 2,3.

L 17

**Text Book:** Topology (Second edition), James R. Munkres, Printice – Hall of India

- 1. Introduction to general Topology K.D Joshi Willey Eastern Limited (1986)
- 2. Topology K.ChandrasekaraRaoNarosa Publishing House New Delhi (2009)

# MSU / 2017-18 / PG -Colleges / M.Sc.(Mathematics ) / Semester -III / Ppr.no.14 / Core-13

### **Advanced Algebra I (75 Hours)**

L	T	P	C
3	2	0	4

### **Objective:**

The aim of the paper is to introduce some of the most fundamental algebraic structures like inner product space, Determinants, etc.

### **Prerequisites:**

Basic knowledge in set theory and Matrix theory

### **Outcome:**

After learning this paper the student can understand,

- The notion of Dual Spaces.
- The algebra of Linear transformations.

**Unit I: Vector spaces:** Dual spaces – Inner product spaces.

**Sections:** 4.3 and 4.4.

L 14

**Unit II:** Linear transformations: The Algebra of linear transformations –

Characteristic roots - Matrices.

**Sections:** 6.1 - 6.3.

L 17

**Unit III:** Canonical Forms: Triangular form – Nilpotent form – Jordan form.

**Sections:** 6.4 - 6.6.

L 16

**Unit IV:** Matrices: Trace and transpose – Determinants.

**Sections:** 6.8-6.9

L 14

**Unit V: Transformations:** Hermitian, unitary and normal transformations.

**Sections:** 6.10(Up to Lemma 6.10.11)

L 14

**Text Book:** Topics in Algebra (Second edition) Wiley Eastern Limited – I.N. Herstein

- A course in Abstract algebra (3<sup>rd</sup> edition)-Vijay.K.Khanna,S.K.Bhambri Vikas Publishing House –Newdelhi.
- Fields and Rings Kaplemsky, Irving (Second edition)-University of Chicago-Chicago (1972).

# MSU / 2017-18 / PG -Colleges / M.Sc.(Mathematics ) / Semester -III / Ppr.no.15 / Core-14

<b>Operations</b>	Research	(75 Hours)
Operanons	11CSCal CII	(15 Hours)

L	T	P	C
3	2	0	4

### **Objectives:**

- To modify rual life into Standard Mathematical Models
- To learn different optimization techniques.
- To know classification of different structured problems.

### **Prerequisite:**

Basic computing knowledge and techniques at undergraduate level.

### **Outcome:**

- Identification of actual problems and its equivalent mathematical models.
- Application to different optimization techniques in real life situations.
- Knowledge gained in utilization of Optimum Resources.

Unit I: Transportation Models And Its Variants: Definition Of The Transportation Model – Nontraditional Transportation Model – Transportation Algorithm – The Assignment Model.

**Chapter 5** – Sections 5.1, 5.2, 5.3, 5.4 and Exercise problems.

L 16

**Unit II:** Network Analysis: Network Definitions – Minimal Spanning Tree Algorithm – Shortest Route Problem – Maximum Flow Model – CPM – PERT.

**Chapter 6** – Sections 6.2, 6.3, 6.4, 6.5, 6.7 and Exercise problems.

L 15

Unit III: Integer Linear Programming: Introduction – Applications – Integer Programming Solutions – Algorithms.

**Chapter 9** – Sections 9.1, 9.2, 9.3 and Exercise problems.

# MSU / 2017-18 / PG -Colleges / M.Sc.(Mathematics ) / Semester -III / Ppr.no.15 / Core-14

Unit IV: Inventory Theory: Basic Elements Of An Inventory Model – Deterministic Models: Single Item Stock Model With And Without Price Breaks – Multiple Items Stock Model With Storage Limitations – Probabilistic Models: Continuous Review Model.

 Chapter 11 – Sections 11.1, 11.2, 11.3, Chapter 16 – Sections 16.1,

 16.2 and Exercise problems.

 L 12

Unit V: Queuing Theory: Basic Elements Of Queuing Model – Role Of Poisson And Exponential Distributions – Pure Birth And Death Models – Specialised Poisson Queues

**Chapter 17** – Sections 17.2, 17.3, 17.4, 17.6(upto 17.6.3) and Exercise problems.

L 15

**Text Book:** Operations Research( Sixth Edition), Hamdy A. Taha, Prentice Hall Of India Private Limited, New Delhi.

- Introduction to Operations Research Fredrick, Shiller, GenraldJ.Literman MC Graw Hill (2017)
- 2. Operations Research KantiSwarup, P.K. Gupta, Man Mohan Sultan Chand and sons. (2016)
- 3. Operations Research (Fifth edition) J.N Sharma, McMillian Publications (2013)

# MSU / 2017-18 / PG -Colleges / M.Sc.(Mathematics ) / Semester -III / Ppr.no.16 / Core-15

L	T	P	C
4	0	0	4

**Research Methodology: (60 Hours)** 

### **Objectives:**

- To understand the Basic aspects in research
- To learn Mathematical and Statistical technique for research
- To acquire basic knowledge about various instruments and techniques in Mathematical research.

### **Prerequisite:**

Basic knowledge in Statistics and related information to be useful for research.

### **Outcome:**

- Training and participating in active research activities for their academic and professional levels.
- Creation of novel ideas and simple technique useful to society(R/D)
- Acquire background knowledge in research publication and thesis writing.

**Unit I:** Research Project: Research Project – Difference between a dissertation and a thesis – Basic requirements of a research degree –Writing a proposal –Ethical considerations

**Chapter 5 :**Sec: 5.1, 5.2, 5.3,5.6,5.13 in Text Book 1.

L10

Unit II: Components of a Research Project: Different components of a research project— Literature review — Methodology — Results / data — Conclusions — Bibliography - Appendices.

**Chapter 6:** Sec: 6.1-6.6,6.7,6.8.1, 6.9.1,6.11, 6.12, 6.13 in Text Book

L10

1.

# MSU / 2017-18 / PG -Colleges / M.Sc.(Mathematics ) / Semester -III / Ppr.no.16 / Core-15

**Unit III:** Some Special Distributions: The Gamma and Chi – Square distribution – The normal distribution.

**Chapter 3:** Sec: 3.3, 3.4 in Text Book 2.

**Exercise Problems: Chapter 3:** 3.28 - 3.33, 3.40 - 3.46.

L13

**Unit IV:** Sampling Theory: Transformation of variables – t & F distributions.

Chapter 4: Sec: 4.1 - 4.4 in Text Book 2.

**Exercise Problems: Chapter 4:** 4.1 - 4.8, 4.14 - 4.17, 4.20 - 4.25,

4.34 - 4.41.

L14

Unit V: Random variables: The MGF technique – Distributions of  $\overline{X}$  and  $\frac{ns^2}{\sigma^2}$  -

Expectations of functions of random variables-The Central Limit Theorem.

**Chapter 4:**Sec : 4.7 – 4.9 in Book 2. **Chapter 5:** Sec 5.4 in Text Book 2

**Exercise Problems: Chapter 4:**4.68 – 4.74, 4.83 – 4.93.

**Exercise Problems: Chapter 5:**, 5.20 - 5.22, 5.25 - 5.27.

L13

**Text Book: 1. Writing up your University Assignments and Research Projects – A Practical handbook,** Neil Murray and Geraldine Hughes, McGraw Hill Open University Press.

**2.Introduction to Mathematical Statistics,** Fourth Edition, Robert V. Hogg and Allen T.Craig, Pearson Education Asia.

- **1.** Research Methodology( 2<sup>nd</sup> revised methods and techniques edition)-C.R.Kothari, New Age International Publications, New Delhi.
- **2.** Fundamentals of Mathematics statistics-S.C.Gupta, V.K.Kapoor, Eleventh edition 2002, Sultanchand& sons Publishers, New Delhi.

 $MSU\,/\,2017\text{-}18\,/\,PG$  –Colleges / M.Sc.(Mathematics ) / Semester -III / Ppr.no.17 / Elective - 2 (a )

Algebraic Number Theory (60 Hours)

L	T	P	С
2	2	0	3

# **Objective:**

- To acquire knowledge about recent developments in Algebra have its impact on Number Theory and Number Theory too has its own contribution to the development of algebra.
- To understand and appreciate the role played by Algebra in Number Theory.

# **Prerequisite:**

Basic knowledge in Distribution of primes, Mathematical Induction and Congruence..

### **Outcome:**

Knowledge gained about various types of numbers such as algebraic Numbers, Pythagorean triples and representation of number as sum of positive squares.

Unit I: Diophantine equations: Diophantine equations – The equation ax+by=c – Positive solutions – Other linear equations.

**Unit II:** Some special equations: The equation  $x^2+y^2=z^2$  – The equation  $x^4+y^4=z^2$ . The equation  $4x^2+y^2=n$ 

Unit III: Infinite continued functions: The equation  $ax^2+by^2+cz^2=0$ - Infinite continued functions – Irrational numbers.

Unit IV: Approximation to irrational numbers : Approximation to irrational numbers- Algebraic integers .

Unit V: Quadratic Fields : Quadratic Fields – Units in quadratic fields.

L 12

**Text book:** An introduction to the theory of Numbers – Ivan Nivan and Herbert **S. Zukerman** – II edition, Wiley Eastern Ltd.

### **Book for Reference:**

Elements of Number Theory – Kumaravelu and SuseelaKumaravelu (2002), Raja Shankar Printers, Sivakasi (V Edition).

# MSU / 2017-18 / PG –Colleges / M.Sc.(Mathematics ) / Semester -III / Ppr.no.17 / Elective - 2 ( b )

# CALCULUS OF VARIATIONS AND INTEGRAL EQUATIONS

**(60 Hours)** 

L	T	P	C
2	2	0	3

**Objective:** 

The objective of this paper is to place at the disposal of the student, the basis of an intelligent working knowledge of a number of facts and techniques which are useful in varied fields of application.

**Prerequisite:** 

Basic knowledge in Elementary Matrix Theory, Quadratic forms, Coordinate Transformations.

**Outcome:** 

Gain knowledge in maxima minima techniques and solution of certain types of Integral equations.

Unit I: Maxima and Minima: Calculus of Variations and Applications – Maxima and

 $\label{lem:minima-lemma} Minima-The\ simplest\ case-Illustrative\ examples.$ 

**Exercises problems:** Chapter 2(2, 6, 8 and 18)

**Sections:** 2.1-2.4

L 11

Unit II: Lagrange's Multipliers: The variational notations – The more general case –

Constraints and Lagrange's Multipliers – Variable end points.

**Exercises problems:** Chapter 2(19, 20 and 21)

**Sections:** 2.5-2.8

L 12

Unit III: Integral Equations: Integral Equations – Introduction – Relation between

differential and integral equations – The Green's function.

**Exercises problems:** Chapter 3(1,9, 11)

**Sections:** 3.1-3.3

L 12

Unit IV: Fredholm equations: Linear Equations in cause and effect- The influence

function -Fredholm equations with separable kernels – Illustrative Examples.

**Exercises problems:** Chapter 3(40 and 43)

**Sections:** 3.5-3.7

L 11

**Unit V:** Hilbert Schmidt theory: Hilbert Schmidt theory – Iterative methods for solving

equations of second kind.

**Exercises problems:** Chapter 3(52 and 53)

**Sections:** 3.8-3.9

L 14

Text Book: Methods of Applied Mathematics, Francis B. Hilde brand,

Prentice Hall of India, New Delhi. Sections: 2.1 to 2.8 and 3.1 to 3.3, 3.5-3.9

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# **Book for Reference:**

Problems and Exercises in integral equations – M.Krarnov, A.Kiselev and G.Makarenko – Mir Publishers, Moscow (1971).

# MSU / 2017-18 / PG –Colleges / M.Sc.(Mathematics ) / Semester -III / Ppr.no.17 / Elective - 2 ( c )

Formal Languages and Automata Theory(60 Hours)

L	T	P	C
2	2	0	3

### **Objectives:**

This course provides a formal connection between algorithmic problems solving and union of languages and automata and develop them into a mathematical view towards algorithmic design and computation.

# **Prerequisite:**

Basic knowledge in computer operations and languages.

### **Outcome:**

- Be able to understand the basic properties of formal languages
- Be able to understand the basic properties of deterministic and non-deterministic finite automata.

# Unit I: Finite automata, regular expressions: Finite state Systems – Basic definitions – Non deterministic finite automata – Finite automata with $\varepsilon$ moves – Regular expressions.

**Chapter 2 :** Sec : 2.1 - 2.5.

**Unit II:** Properties of regular sets: The pumping lemma for regular sets – Closure properties of regular sets – Decision algorithms for regular sets – The Myhill-Nerode Theorem and minimization of finite automata.

**Chapter 3 :** Sec : 3.1 – 3.4

L 12

Unit III: Context - free grammars: Motivation and introduction - Context-free grammars - Derivation trees - Simplification of context-free grammars - Chomsky normal form - Greibach normal form.

**Chapter 4 :** Sec : 4.1 - 4.6

MSU / 2017-18 / PG –Colleges / M.Sc. (Mathematics ) / Semester -III / Ppr.no.17 / Elective - 2 ( c )

**Unit IV: Pushdown automata :** Informal description – Definitions-Pushdown automata and context-free languages.

**Chapter 5 :** Sec : 5.1 - 5.3

L 11

**Unit V:** Properties of context-free languages: The pumping lemma for CFL's – Closure properties for CFL's – Decision algorithms for CFL's.

**Chapter 5:** Sec: 6.1 - 6.3

L 13

**Text Book : Introduction to Automata Theory, Languages and Computation, Jhon E.**Hopcraft and Jeffrey D. Ullman, Narosa Publishing House, New Delhi, 198.

- Introduction to languages & theory of computation John.C.Martin-Tata Mcgraw hill- 2003.
- 2. Introduction to Automata theory ,languages and computation- Hopcraft ,Motwan and Ullman-Pearson publisher- Third edition -2006.
- 3. Elements of the theory of computation-H.R.lewis and C.H.Papadimitrious Tata Mcgraw hill-2003.

**Functional Analysis (90 hours)** 

L	T	P	C
2	4	0	4

### **Objective:**

- To gain knowledge about Banach Spaces, Hilbert Spaces and Banach Algebra.
- To use algebraic structure in Analysis.

### **Prerequisite:**

Basic knowledge of Metric Spaces, Topology and Sequences.

### **Outcome:**

Graduates will have a strong foundations and in depth understanding of the current topics related with functional Analysis, Spectral Theory, Approximation Theory.

**UNIT 1: BanachSpaces:**Banach Spaces- The definition and some examples-Continuous linear transformations- The Hahn Banach Theorem

**Chapter 9** Sections 46, 47, 48.

**Problems:** Section 46 (1-4), 47 (1-3) 48 (1).

L 17

**UNIT 2: Imbedding :** The Natural Imbedding of N in N\*\*- The open

mapping theorem

Chapter 9 Sections 49, 50

**Problems:** Section 49 (1-3), 50 (2,3)

L 18

**UNIT 3: Hilbert Spaces:**Conjugate of an operator -Hilbert Spaces-The Definition and some simple properties- Orthogonal compliments

Chapter 9Section 51, Chapter 10 Sections 52, 53

**Problems:** Section 51 (1-3) 52 (4,6), 53 (1-4).

L 18

**UNIT 4:** The Conjugate space and adjoint: Orthonormal sets-The conjugate space H\*-The Adjoint of an operator- Self adjoint operators

**Chapter 10** Sections 54, 55, 56, 57

**Problems:** Section 54 (1,5) 55 (1-3), 56 (1-4), 57 (1,2)

L 18

**UNIT 5:** Spectral Theory: Normal and Unitary operators- projections, Finite dimensional spectral theory- Determinants and the spectrum of an operator- The spectral theorem

Chapter 10 Sections 58, 59, Chapter 11 Sections 61, 62

**Problems:** Section 58, 59, 61, 62 (1-5).

L 19

**Text Book:** Introduction to Topology and Modern Analysis- G.F. SIMMONS-McGraw-Hill International Editions

- 1. Functional Analysis Second edition (2011), Tata MC Graw Hill Education Private Ltd. (New Delhi) Walter Rudin.
- 2. Functional Analysis K.ChandrasekaraRao, Narosa Publishing House (2009) New Delhi.

L	T	P	C
2	4	0	4

# **Objectives:**

- To gain advanced knowledge about Complex functions and Analytic functions as mappings.
- To understand the concept of Analyticity Conformality, Linear Transformation and Complex Integration.

# **Prerequisite:**

Basic knowledge of concepts of Differentiation and Integration for functions of real variables further in UG level they level the fundamental Ideas and theorems about Complex plane power series residues.

### **Outcome:**

- Acquistation of solving problems in Complex Integration and boundary value problems.
- **Unit I:** Analytic functions : Analytic functions Polynomials Power series Abel's limit theorem.

**Chapter 2:** Sec 1.1 - 1.4, Sec 2.4 & 2.5.

**Problems:** Chapter 2: 1.2 (1,4,5,7) 2.4 (2-6).

L 20

**Unit II:** Conformal mappings: Conformal mappings - Linear transformations – the linear group – the cross ratio- Symmetry – line integrable – line integrable as functions of arc.

**Chapter 3:** Sec 2.3, 3.1 - 3.3, **Chapter 4:** Sec 1.1 - 1.3(1,3,4,5).

**Problems: Chapter 3**: 3.1 (4); 3.2 (1,4) 3.3 (1,2,4);

L 17

Unit III: Cauchy's theorem for Rectangle: Cauchy's theorem for Rectangle - Cauchy's theorem in a disc, Cauchy's Integral formula, Index of a point - The integral formula.

**Chapter 4:** Sec 1.4 & 1.5, 2.1& 2.2

**Problems: Chapter 4** : 2.2 (1-3)

# MSU / 2017-18 / PG -Colleges / M.Sc.(Mathematics ) / Semester -IV / Ppr.no.19 / Core - 17

Unit IV: Higher derivatives -Taylor's Theorem : Higher derivatives -Taylor's Theorem – Zeros and Poles – The local mapping – The maximum principle and the general statement of Cauchy's Theorem (Statement only).

**Chapter 4:** Sec 2.3, 3.1 - 3.4 and 4.4.

**Problems: Chapter 4:** 2.3(1), 3.2(2-4)

L 18

Unit V: Calculus of Residues: Calculus of Residues – The Residue theorem - The Argument Principle – Evaluation of definite integrals.

**Chapter 4:** Sec 5.1 - 5.3

L 19

**Problems: Chapter 4**: 5.2(1-3),5.3 (1, 3(a-g))

**Text:** Complex Analysis – Lars V.Ahlfors – Tata McGraw Hill (Third Edition)

### **Book for Reference:**

Foundations of Complex Analysis – S.Ponnusamy – Narosa Publishing House 2015 (Second Edition).

# MSU / 2017-18 / PG -Colleges / M.Sc.(Mathematics ) / Semester -IV / Ppr.no.20 / Core - 18

**Advanced Algebra II (75 hours)** 

L	T	P	C
3	2	0	4

**Objectives:** 

Gain knowledge in fields in the theory of numbers, the theory of equations and Galois theory .

**Prerequisite:** 

Knowledge of Groups, Rings and Elementary properties of fields.

**Outcome:** 

Understand the application of Galois theory in theory of equations and Geometry.

**Unit I: Extension fields.:** Extension fields.

Sections: 5.1

**Problems:** 5.1(1-5, 8)

L 15

**Unit II:** Roots of polynomials : Roots of polynomials – More about roots.

**Sections:** 5.3, 5.5

**Problems:** 5.5(1-3)

L 16

**Unit III: Elements of Galois theory.:** Elements of Galois theory.

Sections: 5.6

L 16

**Unit IV:** Finite fields : Finite fields – Wedderburn's theorem(First proof

only)

**Sections:** 7.1, 7.2(Theorem 7.2.1-First proof only)

L 14

Unit V: Some special theorems: A theorem of Frobenius – Integral quaternions and

the four square theorem.

**Sections:** 7.3, 7.4.

Text Book: Topics in Algebra (Second edition) Wiley Eastern Limited – I.N. Herstein

- A course in Abstract algebra (3<sup>rd</sup> edition)-Vijay.K.Khanna,S.K.Bhambri Vikas Publishing House –Newdelhi.
- Modern Algebra –Surjeetsingha and Qazizameerudin- Vikas Publishing House –Newdelhi.
- Fields and Rings Kaplemsky, Irving (Second edition)-University of Chicago-Chicago (1972).

**Topology II(75 hours)** 

L	T	P	C
3	2	0	4

### **Objective:**

- Gain knowledge in separation axioms in Topological Spaces.
- Understanding the concepts of Normal and Regular Spaces.

### **Prerequisite:**

- Basic Knowledge in Set theory and Analysis at Undergraduate level.
- Knowledge in first course topology and functions in Topological Spaces.

#### **Outcome:**

• Improves the standard of understanding Set theory, Analysis and Topology and pave the way to do Research in these areas.

**Unit I: Separation axioms.:** The countability axioms – Separation axioms.

Chapter 4: Sections 30, 31.

**Problems:** Section 30: 2,3 and Section 31: 1-3.

L 16

**Unit II:** The Urysohn lemma: Normal spaces – The Urysohn lemma.

Chapter 4: Sections 32, 33.

**Problems:** Section 32: 1, 3, 4 and Section 33: 1-2.

L 15

**Unit III: Urysohn and Tietz extension theorem :** The Urysohn metrization theorem –

The Tietz extension theorem. **Chapter 4:** Sections 34, 35.

**Problems:** Section 34: 1, 3 and Section 35: 1, 3.

L 17

**Unit IV:** The Tychonofftheorem: The Tychonoff theorem - Local finiteness.

**Chapter 5:** Sections 37 and Chapter 6: Section 39

**Problems:** Section 37: 1,2 and Section 39: 3,5.

L 15

**Unit V: Baire Spaces.:** Baire Spaces.

**Chapter 8:** Sections 48.

**Problems:** Section 48: 1, 3, 4, 6.

L 12

**Text Book: Topology** (Second edition), **James R. Munkres**, Printice – Hall of India **Books for reference:** 

- 1. Introduction to General Topology K.D. Joshi Wiley Eastern Limited (1986)
- 2. Topology K.ChandrasekaraRaoNarosa Publishing House 2009 (New Delhi)

# MSU / 2017-18 / PG -Colleges / M.Sc.(Mathematics ) / Semester -IV / Ppr.no.22 / Project

# Project Contact hours -8+

### **Objective:**

- To provide training in scientific skills.
- To prepare students for professional training programme or entry level jobs in any area of Mathematics.

### **Prerequiste:**

 Students should be able to understand and interpret the literature in their areas of research.

### **Outcome:**

At the end of the project the students should have increased

- Their capacity to think critically
- Their ability to design analyse and execute an experiment.
- Their confidence and ability in communication skills(in writing and oral)
- To acquiring the literature collection methods and interpreting the date of their scientific equipment etc.